SDSC SAN DIEGO SUPERCOMPUTER CENTER

EDGE: Benchmarking the Seismic Wave Propagation Solver

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Extreme-scale Discontinuous Galerkin Environment (EDGE)

- **★** Focus: Problem settings with high geometric complexity, e.g., mountain topography
- ★ Unique support for fused simulations exploiting inter-simulation parallelism
- **★** Rapid prototyping through support for: Line elements, guads, triangles, hexes, tets
- ★ Parallelization: Assembly kernels for Sandy Bridge, Bulldozer, Haswell, Knights Corner, Knights Landing, EPYC, Skylake, Knights Mill; OpenMP+MPI (custom and overlapping)
- ★ World record seismic wave propagation performance: 10.4 DP-PFLOPS on Cori Phase II
- ★ Continuity: Continuous Integration (sanity) checks), Continuous Delivery (automated convergence + benchmarks runs), code coverage, license checks, container bootstrap
- ★ License: BSD 3-Clause (software), CC0 for supporting files, e.g., user guide



Illustration of EDGE's modeling and simulation pipel The parallelization is influenced by a multitude of facto The presented verification study is key in determin modeling parameters. Together with other parts of pipeline, highlighted in gray, the study's results dr EDGE's single-core parallelization

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	28	vmovups zmm7, zmmword ptr [rdx+0x1c0] vmovups zmm0, zmmword ptr [rdx+0x200]	12
	20	vmovups zmm9, zmmword ptr [rdx+0x240]	
-	22	vmovups zmml1, zmmaord ptr [rdx+0x2c0]	14
	24	vmovups zmml2, zmmuord ptr [rdx+4x340] vmovups zmml3, zmmuord ptr [rdx+8x340]	16.
	25	vmovups zmm14, zmmword ptr [rdx+0x300] vmovups zmm15, zmmword ptr [rdx+0x3c0]	
	27	vmovups zmm16, zmmaord ptr [rdx+0x400]	18 -
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	28	vmovups zmm20, zmmword ptr [rdi+0x140] vmovups zmm29, zmmword ptr [rdi+0x100]	Top. One out of three stimess
	40	vmovups zmm30, zmmword ptr [rdi+0x1c0]	matricas for totrahadral D2
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	46	vfmadd211ps zmm2, zmm11, dword ptr [rs1+exx/c](1016) vfmadd231ps zmm3, zmm31, dword ptr [rs1+6xa0](1016)	elements in EDGE. Only 77
	42	vmovups zmm20, zmmword ptr [rdi+0x240] vfmadd231ps zmm0, zmm20, dword ptr [rsi+0x10]{1to16}	
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	64 65	<pre>vfmadd231ps zmm6, zmm30, dword ptr [rsi+0xfc]{lto16} ymovuos zmm20, zmmword ptr [rdi+0x3c0]</pre>	Lent: Generated assembly
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	20	véfmaddps zml, zm28, xmmord ptr [rsi+6x64]	
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	16	vfmadd231ps zmm6, zmm31, dword ptr [rs1+6x104]{tto16}	(top) 16 fused simulations
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	80	vfmadd211ps zmm0, zmm11, dword ptr [rs1+ext24](tto16) vfmadd231ps zmm9, zmm31, dword ptr [rs1+6x12c]{tto16}	
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ine.		vfmadd231ps zmn7, zmn28, dword ptr [rsi+0x11c](1to16) vfmadd231ms zmn8, zmn28, dword ptr [rsi+0x1201/[to16]	karnal reaches over 250/ of
	91	vfmadd231ps zmm9, zmm28, dword ptr [rsi+6x130]{lto16}	Kerner reaches over 55% or
orc	92	vnovups znnword ptr [rds+0x40], znn1	
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ive	108	vmovups zmmword ptr [rdx+6x400], zmm16	Right: EDGE's homepage
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XPUG Middle East Conference 2018 at

Fused Simulations Exploit Inter-Simulation Parallelism

"Why is this a good idea?"

- ★ Idea: Exploit input parallelism by fusing multiple, similar simulations in a single execution of the solver
- ★ EDGE supports this idea at all levels of parallelism, starting at a single vector op
- ★ Fusing multiples of the vector-width (KNM, SKX, KNM): 16 simulations in single precision) allows for perfect vectorization without zero ops
- ✤ Fusion of multiples of 64 bytes (16) simulations) leads to alignment to cache-lines without artificial zeropadding
- ★ Read-only data structures are shared among all fused simulations

"Similar simulations?"

- ★ EDGE imposes restrictions on fused seismic simulations: 1) Identical mesh for all fused
 - simulations 2) Identical simulation parameters: start and end time, convergence rate, "frequency" of wave field output, "frequency" and location of seismic receivers 3) Identical material parameters (velocity model)

4) "Sources" mostly arbitrary: Arbitrary initial DOFs, kinematic sources: arbitrary location and moment rates, spontaneous rupture: identical friction law, other initial parameters arbitrary Illustration of EDGE's fused approach (4 simulations), applied to the advection equation with sinusoidal initial values. While a traditional solver handles different initial values in multiple executions, EDGE exploits the input-parallelism and computes the 4 simulations in parallel.

 $q(x,t)_t + v \cdot q(x,t)_x = 0, \ v \in \mathbb{R}$

repository



Illustration of EDGE's memory layout for a third order (P2 elements) ADER-DG solver for the advection equation. In the case of the traditional, non-fused approach, the DG-modes are the fastest dimension in memory, followed by the elements. In case of fused simulations, the fused runs are the fastest dimension, followed by the DG-modes and the elements.

precision are visually indistinguishable.

Motivation of the Study: From Convergence to Verification

Two regular tetrahedral meshes. By imposing periodic **H** Benchmarking is key to assess the accuracy LOH.1 Benchmark: boundary conditions, the plane wave initial solution is of seismic wave propagation solvers Example mesh reproduced after diagonal propagation through the domain, and material even in MPI-parallel settings (right). ★ EDGE has a multitude of modeling regions. parameters: 1) Fused vs. non-fused simulations 2) Single vs. double precision 3) Convergence rate in space and time 4) Feature- and velocity-aware mesh genc refinement 5) Source discretization 6) Topography: Flat vs. DEM-derived 7) Velocity model: Layered vs. data-input MANIN MANY MA **★** Choosing the right modeling parameters is Synthetic seismograms for the ninth receiver and quantity u of the crucial for best time-to-solution LOH.1 wave propagation benchmark. Shown is a comparison of single and double precision arithmetic in EDGE. The left synthetics \star Our verification study considers the entire show fourth order runs, the ones on the right fifth order runs. The modeling and simulation pipeline and Convergence of EDGE for regular, tetrahedral meshes in the two plots on top used a specified characteristic length of 150m, the Linf-norm for the elastic wave equations in velocity-stress form middle plots 175m, and the bottom plots 200m. While higher covers essential modeling decision (1-3 Shown are orders O1-O5 for quantity v (Q8) when utilizing resolutions and orders increase the accuracy, 32bit and 64bit above) for best practices

EDGE's fusion capabilities with shifted initial conditions. [1]

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Implications for High Performance Computing

- ★ Hardware architectures are moving to an era of free computations and expensive data movement
- \star Deep Learning is the new number one driver for hardware developments of all major vendors
- \star Deep Learning hardware increases computation-intensive, reduced precision dense linear algebra capabilities, while sacrificing double precision performance
- ★ Verification study shows: Single precision arithmetic is sufficient for seismic wave propagation using ADER-DG
- \star Fused simulation technology is critical to exploit single precision performance: EDGE increases throughput by 4.2x over SeisSol [3] (16 Knights Mill processors, GTS, 16 fused FP32 simulations, fifth order)



Floating point performance and peak efficiency on 16 nodes. All results Exemplary illustration of EDGE's fourth order solution for the ninth are reported in terms of non-zero operations. Dark gray bars represent the receiver and quantity u of the LOH.1 wave propagation benchmark. Plots performance of single seismic forward simulations, while light gray bars a) and b) show a comparison to the reference, using double precision show the performance of fused simulations. Eight simulations are fused in arithmetic. Out of the eight fused, identical solutions of the setting, only order of convergence, b) computer architecture: Intel Xeon Phi 7250 (knl), identical single and double precision results, obtained when using a single Intel Xeon Phi 7295 (knm), and 2× Intel Scalable Xeon 8180 using AVX512 forward simulation. Dueto the low misfits, shown in d), the FP32 in and (skx) and AVX2 (skx-avx2), c) floating point precision.



Left: Speed-up over the SC 2017 best paper award-

double precision and sixteen in single precision arithmetic. Dimensions: a) the first one is shown. Plots c) and d) show a comparison of the almost FP64 solutions are visually indistinguishable in the raw synthetics c).

Outlook: A Comprehensive Approach

- ★ EDGE-V: Velocity-aware mesh refinement using UCVM shear wave velocities, mesh annotation with velocity model
- **★** EDGEcut: Feature-preserving surface meshing of mountain topography and intersecting fault geometries
- ★ Convergence and verification study of 16bit precision for seismic ADER-DG simulations
- ★ DG subcell-limiter to cope with large gradients in the solution, enabling EDGE for nonlinear hyperbolic PDEs
- ★ Last but not least: If you are interested in working with us, get in touch!



Velocity-aware mesh-refinement using EDGEcut for a modeling domain, which covers the Imperial fault. Contributors: Rajdeep Konwar, Junyi Qiu.

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EDGE heavily relies on contributions of many authors to open-source software This software includes, but is not limited to: ASan (debugger), Catch (unit tests) CGAL (surface meshing), Clang (compiler), Cppcheck (static code analysis) Easyloging ++ (logging), Exprimer), cipclicat (static code analysis), Easyloging ++ (logging), Exprimer), GCC (compiler), Git (versioning), Git LFS (versioning), gitbook (documentation), Gmsh (volume meshing), GMT (DEM pre-processing), GoCD (continuous delivery), HDF5 (I/O) jekyll (homepage), LIBXSMM (matrix kernels), METIS (partitioning), MOAB (mesh interface), NetCDF (I/O), ParaView (visualization), Proj.4 (map projections), pugixml (XML interface), SAGA-Python (automated remote job submission), SCons (build tool), TF-MISFIT GOF CRITERIA (signal analysis), UCVMC (velocity odel), Valgrind (memory debugging), Visit (vis